

Sign Convention: \dot{m} is positive for mass entering the system, \dot{Q}_{cv} is positive for heat transfer to the system, and \dot{W}_{cv} is positive for work done by the system.

Energy Balance: system with mass crossing the boundary at multiple points, neglecting kinetic and potential energy effects

$$\frac{dU}{dt} = \dot{Q}_{cv} - \dot{W}_{cv} + \sum_{j=1}^N \dot{m}_j h_j$$

Entropy Balance: system with mass and heat crossing the boundary at multiple points

$$\frac{dS}{dt} = \sum_{j=1}^N \frac{\dot{Q}_j}{T_j} + \sum_{j=1}^N \dot{m}_j s_j + \dot{\sigma}$$

Boundary Work:

$$\delta W = p dV \quad \text{or for a process } W = \int_1^2 p dV$$

Gibbs Relations

$$ds = du + p dv = dh - v dp$$

Efficiency

$$\eta_{\text{turbine}} = \frac{\dot{W}_{\text{act}}}{\dot{W}_{\text{ideal}}} \quad \eta_{\text{pump}} = \frac{\dot{W}_{\text{ideal}}}{\dot{W}_{\text{act}}}$$

Carnot Efficiency for Heat Engine

$$\eta_{\text{Carnot}} = 1 - \frac{T_L}{T_H}$$

Ideal Gas Property Evaluation:

Changes in enthalpy and internal energy

$$dh = c_p(T) dT \quad \text{and} \quad du = c_v(T) dT$$

$$c_p - c_v = R = \frac{R_u}{MW} \quad \text{and} \quad R_u = 8.314 \text{ kJ/kmol-K}$$

Gibbs Relations

$$ds = c_v dT + p dv = c_p dT - v dp$$

$$ds = c_p \frac{dT}{T} - R \frac{dp}{p}$$

Ideal gas with constant specific heat

$$h_2 - h_1 = c_p (T_2 - T_1)$$

$$u_2 - u_1 = c_v (T_2 - T_1)$$

$$s_2 - s_1 = c_p \ln \left(\frac{T_2}{T_1} \right) - R \ln \left(\frac{p_2}{p_1} \right)$$