

Constant $a = a_c$

$$\begin{aligned}v &= v_0 + a_c t \\s &= s_0 + v_0 t + \frac{1}{2} a_c t^2 \\v^2 &= v_0^2 + 2a_c(s - s_0)\end{aligned}$$

General Expressions (variable α)

$$\begin{aligned}\alpha &= \frac{d\omega}{dt} \\ \omega &= \frac{d\theta}{dt} \\ \omega d\omega &= \alpha d\theta\end{aligned}$$

Constant $\alpha = \alpha_c$

$$\begin{aligned}\omega &= \omega_0 + \alpha_c t \\ \theta &= \theta_0 + \omega_0 t + \frac{1}{2} \alpha_c t^2 \\ \omega^2 &= \omega_0^2 + 2\alpha_c(\theta - \theta_0)\end{aligned}$$

Relative Motion

$$\begin{aligned}\vec{v}_A &= \vec{v}_B + \vec{v}_{A/B} \\ \vec{a}_A &= \vec{a}_B + \vec{a}_{A/B}\end{aligned}$$

General Plane Motion

$$\begin{aligned}\vec{v}_B &= \vec{v}_A + \vec{\omega} \times \vec{r}_{B/A} \\ \vec{a}_B &= \vec{a}_A + \vec{\alpha} \times \vec{r}_{B/A} + \vec{\omega} \times (\vec{\omega} \times \vec{r}_{B/A}) \\ \vec{a}_B &= \vec{a}_A + \vec{\alpha} \times \vec{r}_{B/A} - \omega^2 \vec{r}_{B/A}\end{aligned}$$

Equations of Motion

$$\begin{aligned}\sum \vec{F} &= m\vec{a}_G \\ \sum \vec{M}_G &= I_G \vec{\alpha} \\ \sum \vec{M}_p &= \sum (\mathcal{M}_k)_p\end{aligned}$$

Mass Moments of Inertia

$$\begin{aligned}I_G &= \frac{1}{12} ml^2 \text{ (slender rod)} \\ I_z &= \frac{1}{2} mr^2 \text{ (uniform disk)} \\ I_z &= mr^2 \text{ (thin ring)} \\ I_o &= I_G + md^2 \\ k_G &= \sqrt{\frac{I_G}{m}}\end{aligned}$$

Principle of Work and Energy

$$\begin{aligned}U_{1 \rightarrow 2} &= T_2 - T_1 \\ T &= \frac{1}{2} mv_G^2 + \frac{1}{2} I_G \omega^2 \\ T_1 + V_1 + (U_{1 \rightarrow 2})_{noncons.} &= T_2 + V_2\end{aligned}$$

Principle of Impulse and Momentum

$$\begin{aligned}\sum \int_{t_1}^{t_2} \vec{F} dt &= \vec{p}_2 - \vec{p}_1 \\ \vec{p} &= m\vec{v} \\ \sum \int_{t_1}^{t_2} \vec{M}_G dt &= \vec{H}_{G_2} - \vec{H}_{G_1} \\ \vec{H}_G &= I_G \vec{\omega}\end{aligned}$$

Rotation About Fixed Axis o

$$\begin{aligned}\sum \int_{t_1}^{t_2} \vec{M}_o dt &= \vec{H}_{o_2} - \vec{H}_{o_1} \\ \vec{H}_o &= I_o \vec{\omega}\end{aligned}$$